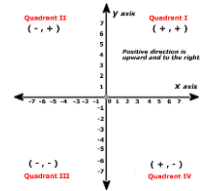


# Chapter 2

Motion in One Dimension

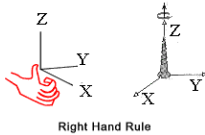
## Cartesian Coordinate System

- The most common coordinate system for representing positions in space is one based on three perpendicular spatial axes generally designated x, y, and z.
- Any point P may be represented by three signed numbers, usually written (x, y, z) where the coordinate is the perpendicular distance from the plane formed by the other two axes.



## Right Hand Rule

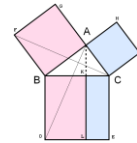
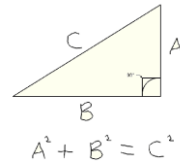
- Point the fingers of your right hand down the positive X axis
- Turn your fingers inward towards the positive Y axis
- Your thumb is now pointing in the positive Z axis



Right Hand Rule

## Pythagorean Theorem

- $a^2 + b^2 = c^2$
- $x^2 + y^2 = z^2$



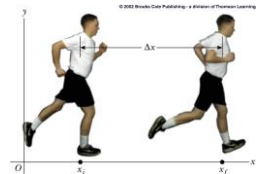
## Distance Formula

- 3-D  
 $d = \sqrt{\Delta x^2 + \Delta y^2 + \Delta z^2}$
- 2-D  
 $d = \sqrt{\Delta x^2 + \Delta y^2}$
- 1-D  
 $d = \sqrt{\Delta x^2} = \Delta x$

Homework: Right Hand Rule - Pythagorean Theorem P.S.

## Position

- Point Particle** - Treat all objects as a single point
- Position** - Where in space an object is located.
- frame of reference** - an arbitrary set of axes with reference to which the position or motion of something is described



## Scalar Quantities

- Scalar quantities are completely described by **magnitude only**
  - **Examples:**
    - 35 meters
    - 40 miles per hour
    - 20 kilograms

## Vector Quantities

- Vector quantities need both magnitude (size) and direction to completely describe them
- **Examples**
  - 35 miles per hour north
  - 20 meters east
- **We can draw vectors**
  - Represented by an arrow, the length of the arrow is proportional to the magnitude of the vector
  - Head of the arrow represents the direction
- **We can identify vector variables:**
  - Generally printed in bold face type

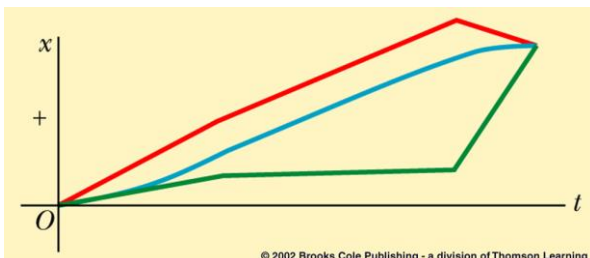
## Displacement

- Measures the change in position
  - Represented as  $\Delta x$  (if horizontal) or  $\Delta y$  (if vertical)
  - **Vector quantity**
    - + or - is generally sufficient to indicate direction for one-dimensional motion
  - Units are meters (m)

## Distance

- Measures how far something has traveled
  - **Scalar quantity**
    - Ignore signs take the absolute values of ever measurement and add them together.
  - Units are meters (m)

## Displacement

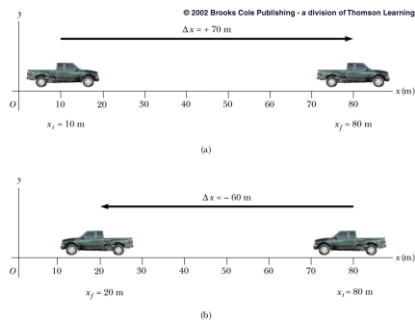


## Distance

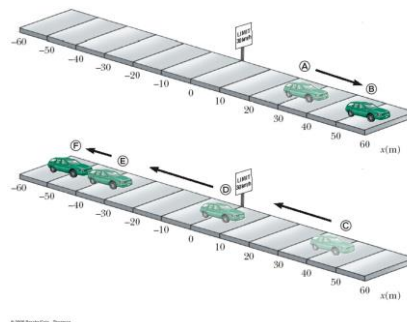


- Distance may be, but is not necessarily, the magnitude of the displacement
- Blue line shows the distance
- Red line shows the displacement

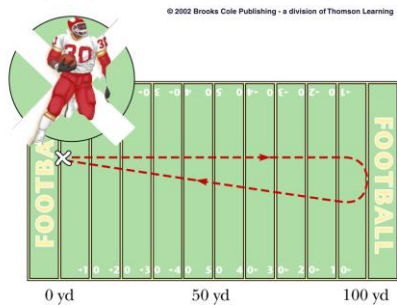
## Displacements vs Distance



## Displacements

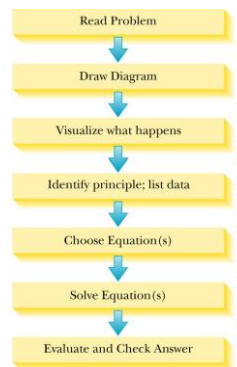


## Football players must be displaced



Homework: Frame of References (Distance vs. Displacement)

## Problem Solving Strategy



## Dynamics

- The sub branch of mechanics that involving the motion of an object and the relationship between that motion and other physics concepts
- **Kinematics** is a part of dynamics
  - In kinematics, you are interested in the *description of motion*
  - *Not concerned with the cause of the motion*

## Brief History of Motion

- Sumaria and Egypt
  - *Mainly motion of heavenly bodies*
- Greeks
  - *Also to understand the motion of heavenly bodies*
  - *Systematic and detailed studies*

## “Modern” Ideas of Motion

- Galileo
  - *Made astronomical observations with a telescope*
  - *Experimental evidence for description of motion*
  - *Quantitative study of motion*

## The idea of variables

- Do not think that a variable always stands for the same concept.
- You must evaluate what you are looking at.
- Example
  - Displacement is represented by (d, x, s, y, z...)

## Velocity

- It takes time for an object to undergo a displacement
- The **average velocity** is rate at which the displacement occurs

$$v_{average} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{\Delta t}$$

- generally use a time interval, so to let  $t_i = 0$
- $\bar{v} = v_{average}$

## Velocity continued

- Direction will be the same as the direction of the displacement (time interval is always positive)
  - + or - is sufficient
- Units of velocity are m/s (SI)
  - Other units may be given in a problem, but generally will need to be converted to these

## Speed

- The **average speed** of an object is defined as the total distance traveled divided by the total time elapsed

$$\text{Average speed} = \frac{\text{total distance}}{\text{total time}}$$

$$v = \frac{d}{t}$$

- Speed is a scalar quantity

## Speed, cont

- Average speed totally ignores any variations in the object's actual motion during the trip
- May be, but is not necessarily, the magnitude of the velocity
- The total distance and the total time are all that is important
- SI units are m/s
  - same units as velocity

## Slope

$$\text{Slope} = \frac{\text{Rise}}{\text{Run}} = \frac{\Delta y}{\Delta x} = \frac{y_f - y_i}{x_f - x_i}$$

Homework: All Velocity and Speed Worksheets

Homework: Slope Worksheets

## Plotting Position vs Time

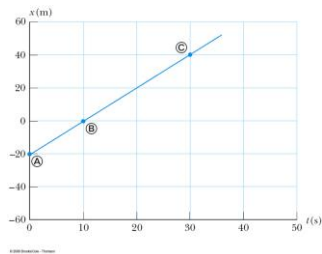
- Dependent Variable- Position
- Independent Variable - Time
- As 1 changes the other changes
- Use Excel

## Graphical Interpretation of Velocity

- Velocity can be determined from a position-time graph
- Average velocity equals the slope of the line joining the initial and final positions
- Compare units of slope
- Instantaneous velocity is the slope of the tangent to the curve at the time of interest
- The instantaneous speed is the magnitude of the instantaneous velocity

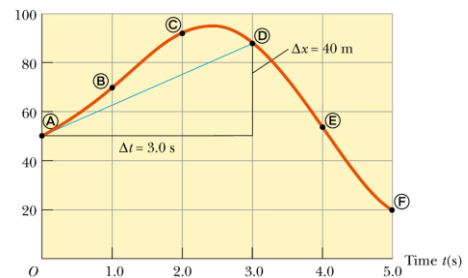
## Average Velocity, Constant

- The straight line indicates constant velocity
- The slope of the line is the value of the average velocity



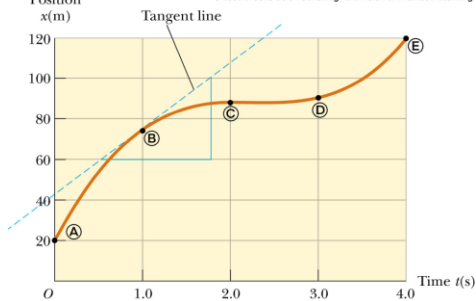
## Average Velocity

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## Instantaneous Velocity

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## Instantaneous Velocity

- The limit of the average velocity as the time interval becomes infinitesimally short, or as the time interval approaches zero

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

- The instantaneous velocity indicates what is happening at every point of time

## Instantaneous Velocity on a Graph

- The slope of the line tangent to the position-vs.-time graph at a point is defined to be the instantaneous velocity at that time
  - The instantaneous speed is defined as the magnitude of the instantaneous velocity

Homework: All Graphical Interpretation of Velocity Worksheets

## Uniform Velocity

- Uniform velocity is constant velocity
- If the instantaneous velocities are always the same
  - All the instantaneous velocities will also equal the average velocity

## Acceleration

- Changing velocity (non-uniform) means an acceleration is present
- Acceleration is the rate of change of the velocity

$$a_{\text{average}} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{\Delta t}$$

- Units are m/s<sup>2</sup> (SI), cm/s<sup>2</sup> (cgs), and ft/s<sup>2</sup> (US Cust)
- Negative acceleration is directional
- Deceleration is just acceleration in the negative direction. Decelerations does not exist

## Average Acceleration

- Vector quantity
- Compare dimensions of velocity vs time graph
- When the sign of the velocity and the acceleration are the same (either positive or negative), then the speed is increasing
- When the sign of the velocity and the acceleration are in the opposite directions, the speed is decreasing

## Time Intervals and displacement

- Objects that are moving equal distances in equal times are moving at constant velocity
- Objects that are not moving equal distances in equal times are accelerating in the positive or negative direction

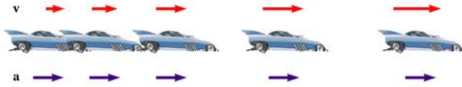
Homework: All Acceleration Worksheets

## Relationship Between Acceleration and Velocity



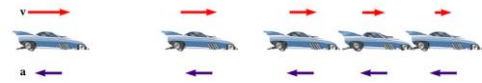
- Uniform velocity (shown by red arrows maintaining the same size)
- Acceleration equals zero

## Relationship Between Velocity and Acceleration



- Velocity and acceleration are in the same direction
- Acceleration is uniform (blue arrows maintain the same length)
- Velocity is increasing (red arrows are getting longer)

## Relationship Between Velocity and Acceleration



- Acceleration and velocity are in opposite directions
- Acceleration is uniform (blue arrows maintain the same length)
- Velocity is decreasing (red arrows are getting shorter)

## Velocity and Acceleration Equations Revisited

$$v_{average} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{\Delta t}$$

$$a_{average} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{\Delta t}$$

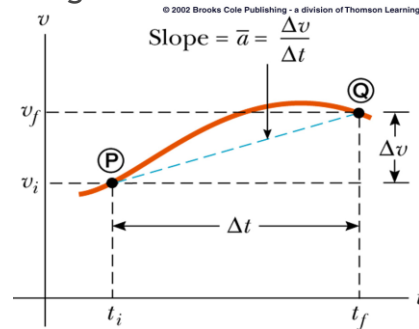
## Instantaneous and Uniform Acceleration

- The limit of the average acceleration as the time interval goes to zero
- When the instantaneous accelerations are always the same, the acceleration will be uniform
  - The instantaneous accelerations will all be equal to the average acceleration

## Graphical Interpretation of Acceleration

- Average acceleration is the slope of the line connecting the initial and final velocities on a velocity-time graph
- Instantaneous acceleration is the slope of the tangent to the curve of the velocity-time graph

## Average Acceleration



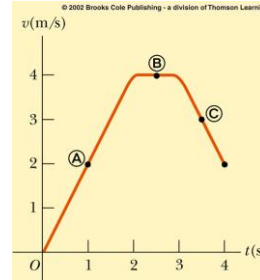
Homework: Velocity and Acceleration Together Worksheets

## Area Under Curves

- The area under a velocity vs time curve is equivalent to the displacement.
- Using the area of a triangle formula
  - $A = 1/2 bh$
 We can determine the displacement from a velocity time graph.

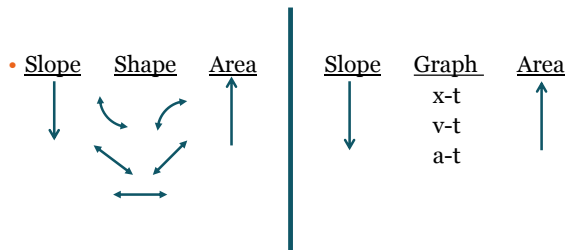
Homework: Area Under Curves Worksheets

## Area Under Curve Practice



Homework: Graphing Displacement, Velocity, and Acceleration Worksheets

## Graph Shapes



Homework: Graphing Displacement, Velocity, and Acceleration Worksheets

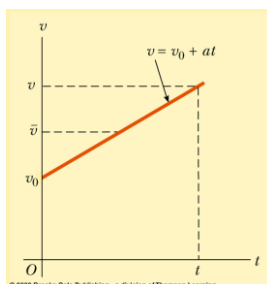
## Derivation of Kinematic equation 1

$$a_{average} = \frac{v_f - v_i}{\Delta t}$$

$$\overline{a} \Delta t = v_f - v_i$$

$$\overline{a} \Delta t + v_i = v_f$$

## Graphical Derivation of Kinematics 1



It is the equation for the slope of the line on a v-t graph

## Kinematic Equation 1

$$V_f = v_o + a * t$$



## Derivation of Kinematics Equation 2

We know Average Velocity

$$\bar{v} = \frac{\Delta d}{\Delta t}$$

Average Velocity is also

$$\bar{v} = \frac{v_o + v_f}{2}$$

But only when acceleration is constant

## Derivation of Kinematics Equation 2

Now substitute Kinematic 1 in for vf

$$\Delta d = \frac{1}{2}(v_o + (v_o + at))\Delta t$$

Now simplify the equation and you get:

$$\Delta d = v_o * t + \frac{1}{2}at^2$$

## Kinematics 2 Alternative Derivation

$$\bar{a}t + v_o = v_f$$

$$d = \frac{1}{2}(v_f - v_o)*t$$

Combining the Equation Above we get:

$$\Delta d = v_o * t + \frac{1}{2}at^2$$

## Derivation of Kinematics Equation 2

Therefore putting it together:

$$\frac{\Delta d}{\Delta t} = \frac{v_o + v_f}{2}$$

Manipulating this equation

$$\Delta d = \frac{1}{2}(v_o + v_f)\Delta t$$

Keep this for Kinematic 3

## Kinematics 2 Alternative Derivation

-If an object is not accelerating then:

$$d = v_o * t$$

Remember that d=area under v vs t graph

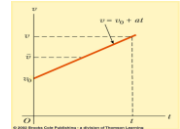
$$\text{area\_of\_Triangle} = 1/2(b)(h)$$

$$\text{area\_of\_Triangle} = 1/2(t)(v_f - v_o)$$

Combining  $v_o t$  we get

$$d = v_o * t + \text{area\_of\_Triangle}$$

$$d = v_o * t + \frac{1}{2}(v_f - v_o)*t$$



## Derivation of Kinematics Equation 3

We start with:  $d = \frac{1}{2}(v_f + v_o)t$

From Kinematic 1 we get

$$t = (v_f - v_i) / a$$

Putting them together we get:

$$d = \frac{1}{2}(v_o + v_f)(v_o - v_f) / a$$

## Derivation of Kinematics Equation 3

Simplifying the equation we get

$$2ad = v_0^2 - v_f^2$$

Solving for  $v_f$  we get:

$$v_f^2 = v_0^2 + 2a\Delta d$$

## Quadratic Equation

- Sometimes we are going to find that we have a quadratic trinomial equation we can't solve. So we use the quadratic solving equation to solve it.
  - The equation should be put into the form:
    - $ax^2 + bx + c = 0$
  - Then solve it with

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Homework: Kinematic and Quadratic Worksheets

## Aristotle

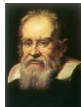
- Greek philosopher, scientist and educator
  - Although most of his contemporaries didn't appreciate his systematical way of performing science westerners later accepted his methods and it is the base of our scientific method

## Aristotle

- Broke motion into 2 parts
  - Natural Motion
    - Things always try to return to their proper place
    - Objects falling speed proportionate to their weight
  - Violent Motion
    - Pushing
    - Pulling
- Earth Centered Universe

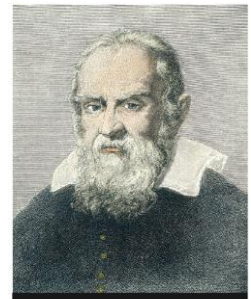
## Time Line

- Aristotle 384-322 BC
- Eratosthenes 276 BC - 200 BC
- Copernicus 2/19/1473- 5/24/1543
- Kepler 12/27/1571- 1630
- Galileo 1564-1642
- Newton 1/4/1643 - 3/31/1727



## Galileo Galilei

- 1564 - 1642
- Galileo formulated the laws that govern the motion of objects in free fall
- Also looked at:
  - Inclined planes
  - Relative motion
  - Thermometers
  - Pendulum



## Free Fall

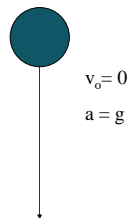
- All objects moving under the influence of only gravity are said to be in free fall
- All objects falling near the earth's surface fall with a constant acceleration
- Galileo originated our present ideas about free fall from his inclined planes
- The acceleration is called the acceleration due to gravity, and indicated by  $g$
- Watch
  - Galileo's Feather

## Acceleration due to Gravity

- Symbolized by  $g$
- $g = 9.8 \text{ m/s}^2$
- $g$  is always directed downward
  - toward the center of the earth

## Free Fall -- an object dropped

- Initial velocity is zero
- Let up be positive
- Use the kinematic equations
  - Generally use  $y$  instead of  $x$  since vertical



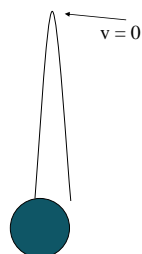
## Free Fall - an object thrown downward

- $a = g$
- Initial velocity  $\neq 0$ 
  - With upward being positive, initial velocity will be negative



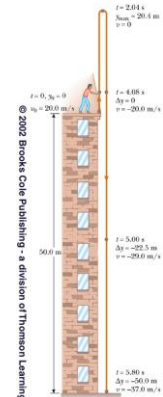
## Free Fall - Object thrown upward

- Initial velocity is upward, so positive
- The instantaneous velocity at the maximum height is zero
- $a = g$  everywhere in the motion
  - $g$  is always downward, negative
- The motion may be symmetrical
  - then  $t_{\text{up}} = t_{\text{down}}$
  - then  $v_f = -v_0$
- The motion may not be symmetrical
  - Break the motion into various parts
    - generally up and down

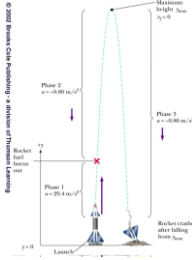


## Non-symmetrical Free Fall

- Need to divide the motion into segments
- Possibilities include
  - Upward and downward portions
  - The symmetrical portion back to the release point and then the non-symmetrical portion

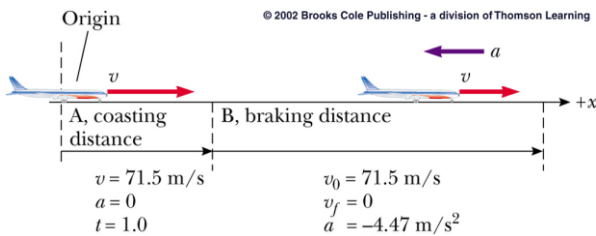


## Combination Motions



Homework: Advanced Kinematic Worksheets

How far does the plane go in the first second? How about once it starts braking?

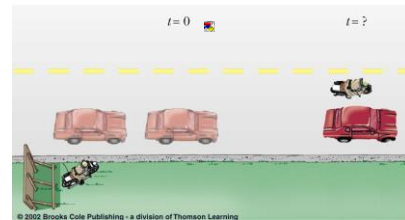


How long does it take the trooper to catch up?

$$v_{\text{car}} = 30.0 \text{ m/s}$$

$$a_{\text{car}} = 0$$

$$a_{\text{trooper}} = 3.00 \text{ m/s}^2$$



## History

- **Eratosthenes of Cyrene (276-200 B.C.)**.. Greek astronomer and mathematician. Calculated the circumference of the Earth and finds a figure of 40,000 km which is close to the present measured value. Also lays down the first lines of longitude on a map of Earth. He also developed a method for calculating all prime numbers: the sieve of Eratosthenes.
- Cosmos 1 – 32 min

## History

- **Eratosthenes of Cyrene (276-200 B.C.)**.

