

Vector Addition Analytically 1

<p>Magnitude of a Vector: $R^2 = R_x^2 + R_y^2 (+R_z^2)$</p> <p>Calculation of x-component R_x: $R_x = R \cos \theta$</p> <p>Calculation of y-component R_y: $R_y = R \sin \theta$</p> <p>Calculation of θ: $\theta = \tan^{-1} \left(\frac{R_y}{R_x} \right)$</p>	<p>Express in Polar Coordinates: [R, θ]</p> <p>Express in Rectangular Coordinates: $R_x \hat{i} + R_y \hat{j}$</p>
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1. Analytically compute the resultant of the following coplanar forces: 100 N @ 30°, 141.4 N @ 45°, and 100 N @ 240°.

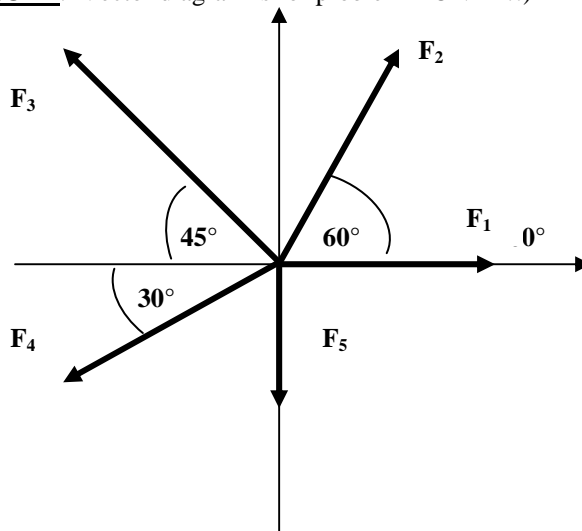
2. If the $w = -5 \hat{i} - 7 \hat{j}$ and $F = 4 \hat{i} - 1 \hat{j}$, then determine the magnitude and direction of the vector sum of these vectors.

3. If $a = 15 @ 80^\circ$ and $b = 12 \hat{i} - 16 \hat{j}$, what is the magnitude and direction of $a - b$?

4. If $a = 25 @ 30^\circ$ and $b = -6 \hat{i} + 14 \hat{j}$, what is the magnitude and direction of $a + b$?

5. Calculate the **resultant** of the following 2 vectors in analytic form: $\mathbf{P} = 2 \text{ m} @ 40^\circ$ and $\mathbf{E} = 4 \text{ m} @ 127^\circ$.

(NOTE: Vector diagram is for problem 2 ONLY!!)



6. Five coplanar forces shown in the diagram at right act on an object. Find their **vector sum resultant**.
 $F_1 = 19 \text{ N}$, $F_2 = 15 \text{ N}$, $F_3 = 16 \text{ N}$, $F_4 = 11 \text{ N}$, $F_5 = 22 \text{ N}$
(NOTE: NOT DRAWN TO SCALE!)

7. Using the analytical method, find the magnitude and direction of the resultant of the following
- 16 m @ 67° ;
 - 30m @ 232°

8. Using the analytical method, find the magnitude and direction of the resultant of the following
- 10 m @ 45° ;
 - 15 m @ 315°

9. Using the analytical method, find the magnitude and direction of the resultant of the following:

$$\vec{r}_1 = 5m @ 135^\circ$$

$$\vec{r}_2 = 8m @ 290^\circ$$

$$\vec{r}_3 = 3m @ 25^\circ$$

$$\vec{r}_4 = (2\hat{i} - 2\hat{j})m$$

10. Using the analytical method, find the magnitude and direction of the resultant of the following:

$$\vec{r}_1 = 8m @ 235^\circ$$

$$\vec{r}_2 = 5m @ 190^\circ$$

$$\vec{r}_3 = 4m @ 5^\circ$$

$$\vec{r}_4 = (2\hat{i} - 6\hat{j})m$$