

Projectile Motion Variable Notes

2D Projectile Motion variables, their meanings, and their functions.

v_o = initial velocity at the beginning of the problem. (answers how fast and in what direction.)

θ = the launch angle (answers in what direction was the projectile launched.)

v_{ox} = initial velocity in the x-direction at the beginning of the problem
(answers how fast in the x- direction at $t = 0$ sec.)

v_{oy} = initial velocity in the y-direction at the beginning of the problem.
(answers how fast in the y- direction at $t = 0$ sec.)

Δx = horizontal displacement at any moment in time.
(answers how far in the x- direction at any moment in time.)

Δy = vertical displacement at any moment in time.
(answers how far in the y- direction at any moment in time.)

y_{MAX} = **maximum** height or altitude of the projectile (use Δy in your equations.)
(This is a special value of Δy .)

R = range of the projectile, which is the **maximum** horizontal displacement of the projectile.
(This is a special value of Δx .)

t_{TOT} = total air time of the projectile. (answers how long the event took to occur.)

t_r = time it takes the projectile to reach y_{MAX} .

v_f = final impact velocity of the projectile. (find vector components v_{fx} and v_{fy})
(answers how fast the projectile is traveling upon impact.)

v_{fx} = final impact velocity in the x-direction of the projectile. (numerically equal to v_{ox})

v_{fy} = final impact velocity in the y-direction of the projectile. (changes in time due to gravity)

2D Projectile Motion Equations:

x-direction: $\Delta x = v_{ox} t$

y-direction: $v_y = v_{oy} - gt$
 $\Delta y = v_{oy}t - \frac{1}{2}gt^2$
 $v_y^2 = v_{oy}^2 - 2g\Delta y$

NOTES:

- When a projectile is thrown horizontally, initially it is moving horizontally, **NOT** vertically... therefore, $v_{oy} = 0$ for these types of problems.
- When the problem states that the projectile *starts and stops on the same level*, assume $\Delta y = 0$ (Symmetrical!!).
- In the absence of drag, maximum range is achieved at a 45° angle and maximum altitude is achieved at a 90° angle.
- The launch angle θ and the initial velocity v_o are the *most important variables* to have. If you do not have these variables at the start of the problem, **FINDING THEM IS OF THE UTMOST IMPORTANCE!!**