Experiment 6: Convex and Concave Lenses

Required Equipment from Basic Optics System

- Light Source
- Convex Lens from Ray Optics Kit
- Concave Lens from Ray Optics Kit

Other Required Equipment

- Metric ruler

Purpose

In this experiment, you will explore the difference between convex and concave lenses and determine their focal lengths.

Theory

When parallel light rays pass through a thin lens, they emerge either converging or diverging. The point where the converging rays (or their extensions) cross is the focal point of the lens. The focal length of the lens is the distance from the center of the lens to the focal point. If the rays diverge, the focal length is negative.

Procedure

1. Place the light source in ray-box mode on a white sheet of paper. Turn the wheel to select three parallel rays. Shine the rays straight into the convex lens (see Figure 6.1).

   Note: The lenses used in this experiment have one flat edge. Place the flat edge on the paper so the lens stands stably without rocking.

2. Trace around the surface of the lens and trace the incident and transmitted rays. Indicate the incoming and the outgoing rays with arrows in the appropriate directions.

3. The point where the outgoing rays cross is the focal point of the lens. Measure the focal length from the center of the lens to the focal point. Record the result in Table 6.1.

4. Repeat the procedure with the concave lens. Note that in step 3, the rays leaving the lens are diverging and do not cross. Use a ruler to extend the outgoing rays straight back through the lens. The focal point is where these extended rays cross. (Remember to record the focal length as a negative number.)

<table>
<thead>
<tr>
<th>Table 6.1: Results</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Convex Lens</strong></td>
</tr>
<tr>
<td><strong>Concave Lens</strong></td>
</tr>
<tr>
<td>Focal Length</td>
</tr>
</tbody>
</table>
5. Nest the convex and concave lenses together and place them in the path of the parallel rays (see Figure 6.2). Trace the rays. Are the outgoing rays converging, diverging or parallel? What does this tell you about the relationship between the focal lengths of these two lenses?

6. Slide the convex and concave lenses apart by a few centimeters and observe the effect. Then reverse the order of the lenses. Trace at least one pattern of this type. What is the effect of changing the distance between the lenses? What is the effect of reversing their positions?
Experiment 8: Lensmaker’s Equation

Purpose

In this experiment you will determine the focal length of a concave lens in two ways: 
a) by direct measurement using ray tracing and b) by measuring the radius of curvature 
and using the lensmaker’s equation.

Theory

The lensmaker’s equation is used to calculate the focal length (in air or a vacuum), \( f \),
of a lens based on the radii of curvature of its surfaces \( R_1 \) and \( R_2 \) and the index of 
refraction \( n \) of the lens material:

\[
\frac{1}{f} = (n - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)
\]

In this notation, \( R \) is positive for a convex surface (as viewed from outside the lens) 
and \( R \) is negative for a concave surface (as in Figure 8.1).

Procedure

1. Place the light source in ray-box mode on a white sheet of paper. Turn the wheel 
to select three parallel rays. Shine the rays straight into the convex lens (see Figure 8.2).

\Note: The lens has one flat edge. Place the flat edge on the paper so the lens stands stably 
without rocking.
2. Trace around the surface of the lens and trace the incident and transmitted rays. Indicate the incoming and the outgoing rays with arrows in the appropriate directions.

3. Remove the lens. To measure the focal length, use a ruler to extend the outgoing diverging rays straight back through the lens. The focal point is where these extended rays cross. Measure the distance from the center of the lens to the focal point. Record the result as a negative value:

\[ f = \text{__________} \text{(measured directly)} \]

4. To determine the radius of curvature, put the concave lens back in the path of the rays and observe the faint reflected rays off the first surface of the lens. The front of the lens can be treated as a concave mirror having a radius of curvature equal to twice the focal length of the effective mirror (see Figure 8.3).

Trace the surface of the lens and mark the point where the central ray hits the surface. Block the central ray and mark the point where the two outer rays cross. Measure the distance from the lens surface to the point where the reflected rays cross. The radius of curvature is \textit{twice} this distance. Record the radius of curvature:

\[ R = \text{__________} \]

5. For this lens, it is not necessary to measure the curvature of both sides because they are equal \((R_1 = R_2 = R)\). Calculate the focal length of the lens using the lensmaker’s equation (Equation 8.1). The index of refraction is 1.5 for the acrylic lens. Remember that a concave surface has a negative radius of curvature.

\[ f = \text{__________} \text{(calculated)} \]

6. Calculate the percent difference between the two values of \(f\) from step 3 and step 5:

\[ \% \text{ difference} = \text{__________} \]
Experiment 12: Focal Length and Magnification of a Thin Lens

Required Equipment from Basic Optics System
- Light Source
- Bench
- Converging lens of unknown focal length
- Screen

Other Equipment
- Metric ruler
- Optics Caliper (optional, for measuring image sizes), PASCO part OS-8468

1Instructors: see note on page 63.

Purpose
The purpose of this experiment is to determine the focal length of a thin lens and to measure the magnification for a certain combination of object and image distances.

Theory
For a thin lens:

\[
\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i}
\]

where \( f \) is focal length, \( d_o \) is the distance between the object and the lens, and \( d_i \) is the distance between the image and the lens. By measuring \( d_o \) and \( d_i \), the focal length can be determined.

Magnification, \( M \), is the ratio of image size to object size. If the image is inverted, \( M \) is negative.

Part I: Object at Infinity
In this part, you will determine the focal length of the lens by making a single measurement of \( d_i \) with \( d_o \equiv \infty \).

Procedure
1. Hold the lens in one hand and the screen in the other hand. Focus the image of a distant bright object (such as a window or lamp across the room) on the screen.

2. Have your partner measure the distance from the lens to the screen. This is the image distance, \( d_i \).

\[ d_i = \text{______________} \]

Analysis
1. As \( d_o \) approaches infinity, what does \( 1/d_o \) approach?
2. Use the Thin Lens Formula (Equation 12.1) to calculate the focal length.

\[ f = \quad \text{______________} \]

Part II: Object Closer Than Infinity

In this part, you will determine the focal length by measuring several pairs of object and image distances and plotting \( \frac{1}{d_o} \) versus \( \frac{1}{d_i} \).

![Figure 12.1](image)

Procedure

1. Place the light source and the screen on the optics bench 1 m apart with the light source’s crossed-arrow object toward the screen. Place the lens between them (see Figure 12.1).

2. Starting with the lens close to the screen, slide the lens away from the screen to a position where a clear image of the crossed-arrow object is formed on the screen. Measure the image distance and the object distance. Record these measurements (and all measurements from the following steps) in Table 12.1.

3. Measure the object size and the image size for this position of the lens.

4. Without moving the screen or the light source, move the lens to a second position where the image is in focus. Measure the image distance and the object distance.

5. Measure the object size and image size for this position also. Note that you will not see the entire crossed-arrow pattern. Instead, measure the image and object sizes as the distance between two index marks on the pattern (see Figure 12.2 for example).

6. Repeat steps 2 and 4 with light source-to-screen distances of 90 cm, 80 cm, 70 cm, 60 cm, and 50 cm. For each light source-to-screen distance, find two lens positions where clear images are formed. (You don’t need to measure image and object sizes.).

Analysis Part A: Focal Length

1. Calculate \( \frac{1}{d_o} \) and \( \frac{1}{d_i} \) for all 12 rows in Table 12.1.

2. Plot \( \frac{1}{d_o} \) versus \( \frac{1}{d_i} \) and find the best-fit line (linear fit). This will give a straight line with the x- and y-intercepts equal to \( \frac{1}{f} \). Record the intercepts (including units) here:

- y-intercept = \( \frac{1}{f} = \text{______________} \)
- x-intercept = \( \frac{1}{f} = \text{______________} \)

Note: You can plot the data and find the best-fit line on paper or on a computer.
3. For each intercept, calculate a value of $f$ and record it in Table 12.2.

4. Find the percent difference between these two values of $f$ and record them in Table 12.2.

5. Average these two values of $f$. Find the percent difference between this average and the focal length that you found in Part I. Record these data in Table 12.2.

<table>
<thead>
<tr>
<th>Table 12.2: Focal Length</th>
</tr>
</thead>
<tbody>
<tr>
<td>Result from x-intercept</td>
</tr>
<tr>
<td>Result from y-intercept</td>
</tr>
<tr>
<td>% difference between results from intercepts</td>
</tr>
<tr>
<td>Average of results from intercepts</td>
</tr>
<tr>
<td>Result from Part I</td>
</tr>
<tr>
<td>% difference between Average of results from intercepts and result from Part I</td>
</tr>
</tbody>
</table>

**Analysis Part B: Magnification**

1. For the first two data points only (the first two lines of Table 12.2), use the image and object distances to calculate the magnification, $M$, at each position of the lens. Record the results in Table 12.3.

$$M = \left( \frac{d_i}{d_o} \right)$$  \hspace{1cm} (eq. 12.2)
2. Calculate the absolute value of $M$ (for each of the two lens positions) using your measurements of the image size and object size. Record the results in Table 12.3.

\[ |M| = \frac{\text{image size}}{\text{object size}} \]  

3. Calculate the percent differences between the absolute values of $M$ found using the two methods. Record the results in Table 12.3.

<table>
<thead>
<tr>
<th>Table 12.3: Magnification</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Point 1</strong></td>
</tr>
<tr>
<td>$M$ calculated from image and object distances</td>
</tr>
<tr>
<td>$</td>
</tr>
<tr>
<td>% difference</td>
</tr>
</tbody>
</table>

Questions

1. Is the image formed by the lens upright or inverted?

2. Is the image real or virtual? How do you know?

3. Explain why, for a given screen-to-object distance, there are two lens positions where a clear image forms.

4. By looking at the image, how can you tell that the magnification is negative?

5. You made three separate determinations of $f$ (by measuring it directly with a distant object, from the x-intercept of your graph, and from the y-intercept). Where these three values equal? If they were not, what might account for the variation?
Experiment 14: Virtual Images

Required Equipment from Basic Optics System

Light Source
Bench
-150 mm lens
+200 mm lens
Viewing screen
Concave/convex Mirror
Half-screen

Other Equipment
Tape

Purpose

In this experiment, you will study virtual images formed by a diverging lens and a convex mirror.

Theory

A virtual image cannot be viewed on a screen. It forms where the backwards extensions of diverging rays cross. You can see a virtual image by looking at it through a lens or mirror. Like all images, a virtual image formed by a lens or mirror can serve as the object of another lens or mirror.

Part I: Virtual Image Formed by a Diverging Lens

In this part, you will set up a diverging lens to form a virtual image. You will then use another lens to form a real image of the virtual image. In this way you can identify the location of the virtual image.

Procedure

1. Place the -150 mm lens on the bench at the 30 cm mark.
2. Place the light source at the 10 cm mark with the crossed-arrow object toward the lens.
3. Record the object distance $d_{o1}$ (the distance between the light source and the lens) in Table 14.1.
4. Look through the lens toward the light source (see Figure 14.1). Describe the image. Is it upright or inverted? Does it appear to be larger or smaller than the object?

________________________________________________________________
________________________________________________________________

5. Which do you think is closer to the lens: the image or the object? Why do you think so?

________________________________________________________________
________________________________________________________________

6. Place the +200 mm lens on the bench anywhere between the 50 cm and 80 cm marks. Record the position here. _____________

7. Place the viewing screen behind the positive lens (see Figure 14.2). Slide the screen to a position where a clear image is formed on it. Record the position here. _____________

![Figure 14.2](image)

The real image that you see on the screen is formed by the positive lens with the virtual image (formed by the negative lens) acting as the object. In the following steps, you will discover the location of the virtual image by replacing it with the light source.

8. Remove the negative lens from the bench. What happens to the image on the screen?

________________________________________________________________

9. Slide the light source to a new position so that a clear image is formed on the screen. (Do not move the positive lens or the screen.) Write the bench position of the light source here. _____________

![Figure 14.3](image)
Analysis

The current position of the light source is identical to the previous position of the virtual image.

1. Calculate the virtual image distance \(d_{i1}\) (the distance between the negative lens and the virtual image). Remember that it is a negative. Record it in Table 14.1.

2. Calculate the magnification and record it in Table 14.1.

\[
M_1 = \frac{d_{i1}}{d_{o1}}
\]

Table 14.1: Negative Lens

<table>
<thead>
<tr>
<th>(d_{o1})</th>
<th>(d_{i1})</th>
<th>(M_1)</th>
</tr>
</thead>
</table>

Questions

1. How do you know that the current position of the light source is identical to the position of the virtual image when the negative lens was on the bench?

2. In step 5 of the procedure, you predicted the position of the virtual image relative to the light source. Was your prediction correct?

3. Is \(M_1\) positive or negative? How does this relate to the appearance of the image?

4. Draw a scale diagram showing the light source in its original position, both lenses, the screen, and both images. Label every part.

5. Draw another diagram at the same scale showing the light source in its final position, the positive lens, the screen, and the image.

Part II: Virtual Image Formed by a Convex Mirror

In this part, you will find the location of a virtual image formed by convex mirror.

Procedure

1. Stick a piece of tape to the viewing screen and draw a vertical line on it as shown in Figure 14.4.

2. Place the half-screen on the bench near one end. Turn the screen so its edge is vertical (see Figure 14.5).

3. Place the concave/convex mirror on the bench, about 20 cm from the half-screen, with the convex side facing the half-screen.
4. Look through the half-screen into the mirror. Describe the image of the half-screen. Is it upright or inverted? Does it appear to be larger or smaller than the object?

________________________________________________________________
________________________________________________________________
________________________________________________________________

5. Guess where the image is. Place the viewing screen on the bench at this location (see Figure 14.6).

In the following steps, you will adjust the position of the viewing screen so that it is in the same place as the virtual image.

6. Look over the top of the half-screen (Figure 14.7a) so that you can see the virtual image of the half-screen and the line drawn on the viewing screen at the same time (Figure 14.7b).

7. Move your head left and right by a few centimeters. If the line on the viewing screen and the image of the half-screen are not at the same distance from your eye, they will appear to move relative to each other. This effect is known as parallax.

8. Adjust the position of the screen and check for parallax again. Repeat this step until there is no parallax between the line and the image. When you move your head, they should appear to be “stuck” together.

Analysis

The viewing screen is now in the same location as the virtual image.

1. Record the object distance $d_o$ in Table 14.2.

2. Calculate the image distance $d_i$ (the distance between the mirror and the virtual image). Remember that it is a negative. Record it in Table 14.2.
3. Use $d_o$ and $d_i$ to calculate the magnification and record it in Table 14.1.

<table>
<thead>
<tr>
<th>Table 14.2: Convex Mirror</th>
</tr>
</thead>
<tbody>
<tr>
<td>$d_o$</td>
</tr>
<tr>
<td>$d_i$</td>
</tr>
<tr>
<td>$M$</td>
</tr>
</tbody>
</table>

Questions

1. Is the magnitude of $d_i$ less than or greater than $d_o$? If you replace the convex mirror with a plane mirror, what would be the relationship between $d_i$ and $d_o$?

2. Is $M$ positive or negative? How does this relate to the appearance of the image?

3. Draw a scale diagram showing the half-screen, mirror, viewing screen, and virtual image. Label every part.